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Amendments to the Specification

Page 1, line 4, delete the paragraph consisting of: "Arthur Torosyan".

Page 1, please modify the two paragraphs at lines 16-19 as follows:

Apparatus and Method for Trigonometric Interpolation," ~~Attorney Docket No.~~ ~~1904.0140001~~ U.S. Patent Application Serial No. 09/699,088, filed October 30, 2000; and

Apparatus and Method for Angle Rotation," ~~Attorney Docket No. 1904.0140001~~ U.S. Patent Application Serial No. 09/698,246, filed October 30, 2000.

Page 3, please modify the paragraph beginning at line 19 as follows:

For proper operation, these third generation systems require proper synchronization between the transmitter and the receiver. More specifically, the frequency and phase of the receiver local oscillator should substantially match that of the transmitter local oscillator. When there is a mismatch, then an undesirable rotation of the symbol constellation will occur at the receiver, which will seriously degrade system performance. When the carrier frequency offset is much smaller than the symbol rate, the phase and frequency mismatches can be corrected at baseband by using a phase rotator. It is also necessary to synchronize the sampling clock such that it extracts symbols at the correct times. This can be achieved digitally by performing appropriate digital ~~resamples~~ resampling.

Page 6, please replace the paragraph at line 14 with the following:

FIG. 3 illustrates [a] Lagrange basis polynomials.

Page 7, please modify the paragraph beginning at line 14 as follows:

FIG. 16A-D illustrates a comparison of the amount of interpolation error using

(A) ~~Language~~ Lagrange cubic, (B) the trigonometric interpolator 1000, (C) the

trigonometric interpolator <u>1400</u>, (D) the optimal structure (to be discussed in Section 4).

Page 8, please modify the paragraph beginning at line 24 as follows:

FIG. 33 illustrates <u>a</u> signal with two samples/symbol and 40% excess bandwidth

<u>according to</u> embodiments of the present invention.

Pages 9-10, please modify the six paragraphs beginning at line 27 on page 9 as follows:

FIG. 49 illustrates a Booth multiplier ~~according to embodiments of the present~~

~~invention~~.

FIG 50 illustrates an original Booth table 5000.

FIG. 51 illustrates ~~an~~ <u>a</u> negating ~~booth~~ <u>Booth</u> table 5100 according to

embodiments of the present invention.

FIG 52 illustrates [an] <u>a</u> negating Booth multiplier 5200.

FIG. 53 illustrates a conditionally negating Booth decoder 5300 <u>according to</u>

<u>embodiments of the present invention</u>.

FIG. 54 illustrates a conditionally negating multiplier 5400 <u>according to</u>

<u>embodiments of the present invention</u>.

Page 10, please modify the two paragraphs beginning at line 25 as follows:

FIG. 64[.] illustrates <u>simultaneous operation of</u> a <u>symbol-timing</u> synchronizer<u> and</u> <u>a carrier phase recovery system</u> 6400 according to embodiments of the present invention.

FIG. 65A-65B illustrate a flowchart ~~6200~~ <u>6500</u> associated with the synchronizer ~~6100~~ <u>6400</u> according to embodiments of the present invention.

Page 11, please modify the paragraph beginning at line 12 as follows:

FIGs. 75A-B illustrate impulse responses of the non-center-interval interpolation filter (A) before and ~~(b)~~ <u>(B)</u> after optimization, according to embodiments of the present invention.

Page 29, please modify the paragraph beginning at line 22 as follows:

FIG. 10 illustrates [an] <u>a</u> trigonometric interpolator 1000 that is one circuit configuration that implements the trigonometric interpolator equations (2.9)-(2.11), where the number of data samples is N=4. The interpolator 1000 is not meant to be limiting, as those skilled in the arts may recognize other circuit configurations that implement the equations ~~(2.8)~~<u>(2.9)</u> - (2.11). These other circuit configurations are within the scope and spirit of the present invention.

Page 30, please modify the paragraph beginning at line 6 as follows:

The adder/subtractor module 1006 includes multiple adders (or subtractors) 1014, where subtraction is indicated by a (-) ~~signs~~ sign.

Page 30, please modify the paragraph beginning at line 19 as follows:

In step 1706, the adder/subtractor module 1006 generates one or more trigonometric coefficients according to the equation (2.9). In FIG. 10, the coefficients are represented by C_0, C_1, and C_2 for N=4, where the ~~coefficients~~ coefficient C_1 is a complex coefficient ~~coefficients~~.

Page 31, please modify the paragraph beginning at line 11 as follows:

The trigonometric interpolator is not limited to the 4th degree embodiment that is shown in FIG. 10. The trigonometric interpolator can be configured as an Nth degree interpolator based on N_data points, as represented by the equations (2.9)-(2.11). These other Nth degree interpolators are within the scope and spirit of the present invention. For example and without limitation, FIG. 11 illustrates an ~~interpolotor~~ interpolator 1100 having N=8. The trigonometric interpolator 1100 includes: a delay module 1102, an adder/subtractor module 1104 (having two scaling multipliers having coefficients cos (π/4)), an angle rotator module 1106, and an adder 1108_(having [an] a 1/8 scale factor that is not shown). The operation of the interpolator 1100 will be understood by those skilled in the arts based on the discussion herein.

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Page 33, please amend the paragraph beginning at line 13 as follows:

The critical path of the Farrow structure 400 (FIG. [2] 4) are is now compared to that of the trigonometric interpolator. The Farrow structure implements the Lagrange interpolator as discussed above. The Farrow structure 400 is shown in FIG. 9_(or FIG. 4), with the critical path 902 indicated. The critical path 902 for this structure includes one scaling multiplier 904 and $N - 1$ data multipliers 906.

Page 37 , please amend the two paragraphs beginning at line 7 as follows:

In step 1908, the adder/subtractor module 1402 generates one or more trigonometric coefficients according to modifications to the equation ([2.8]2.9). In the N=4 case, equations (2.25) are implemented by the module 1402. In FIG. 14, for N=4, the coefficients are represented by C_0 and C_1, where the coefficient C_1 is a complex coefficient coefficients. By comparing with FIG. 10, it is noted that the C_2 coefficient is 0. Additionally, the adder/subtractor module 1402 outputs the K value for further processing. Notice also that in FIG. 14, the output scaling factor has been changed from ¼ to ½. This reflects several other straightforward simplfications simplifications that have been made to module 1402 and in the angle rotator 1010b. In embodiments, the steps 1906 and 1908 are to be preformed performed simultaneously by the adder/subtractor module 1402, as will be understood by those skilled in the relevant arts.

In step 1910, the angle rotator 1010b rotates the complex coefficient C_1 in a complex plane according the offset μ, resulting in a rotated complex coefficient. In

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embodiments, as discussed herein, the angle rotator[s] 1010b is table look-up. In which

case, a complex rotation factor is ~~retrieve~~ retrieved from the table lookup based on the

offset μ, and the resulting rotation factor is then multiplied by the corresponding complex

coefficient, to generate the respective rotated complex coefficient. The rotation factor

includes the evaluation of the cosine and sine factors that are shown in equations (2.21).

Note that since $C_2 = 0$, the angle rotator 1010a is replaced with the multiplier 1404.

Page 38, please amend the paragraph beginning at line 6 as follows:

The simplified trigonometric interpolator is not limited to the four-sample

embodiment that is shown in FIG. 14. The simplified trigonometric interpolator can be

configured as an N-sample interpolator based on N[-]_data points, as represented by the

equations (2.28)-(2.30). These other N-sample interpolators are within the scope and

spirit of the present invention. For example and without limitation, an interpolator with

N=8 is discussed below.

Page 39, please amend the paragraph beginning at line 5 as follows:

How does the simplified interpolator 1400 (FIG. 14) perform as compared to the

interpolator 1000 (FIG. 10)? FIGs. 16A-C show the frequency responses, in solid lines,

of the Lagrange cubic interpolator 400 (FIG. [14]4), the interpolator 1000 (FIG.10) and

the simplified interpolator 1400 (FIG. 14), respectively. For an input signal whose

spectrum is a raised cosine with α=0.4, as shown in dashed lines, the amount of

interpolation error corresponds to the gray areas. Clearly, the interpolator 1400 produces

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less error than the Lagrange cubic interpolator 400 and the interpolator 1000. (FIG. 16D
will be discussed in Section 4.)

Page 41, please amend the two paragraphs beginning at line 1 as follows:

We can easily adapt the trigonometric interpolator described herein to efficiently

create such a sampling rate conversion system, but one that does not require such

filtering operations. If we denote the integer factor by which we desire to increase the

data rate as L (in the above example, L = 4) we proceed as follows. We build the system

7800 shown below in Fig.78[)]. System 7800 includes a Delay Module 7802 and

Add/Subtract Module 7804 (that are similar to ~~that~~ those in FIG. 10), and such that it can

accommodate incoming data at a rate r. We now build L copies of the Angle-Rotation

Module 7806 (similar to that in FIG. 10), with each one being fed by the same outputs of

the Add/Subtract Module. Within each of these L Angle-Rotation Modules 7806 we fix

the μ value; that is, each one has ~~one has~~ a different one of the values: 1/L, 2/L,..., (1-

L)/L. With such fixed μ values, each Angle-Rotation Module 7806 can be constructed as

a set of fixed multipliers (a very special case of the table-lookup method), although any

of the Angle-Rotation Module implementations previously discussed can be employed.

As shown in Fig. 78, the L-1 outputs, i.e., the interpolated samples that are offset

by the values 1/L, 2/L,..., (L-1)/L from the first of the two data points (indicated as μ = 0

and μ = 1 in the Delay Module of Fig. [A] 78) are routed to a multiplexer 7808, along

with the input data point from which all interpolated samples are offset. The multiplexer

7808 simply selects these samples, in sequence, and provides them to the output at the

expanded data rate L x r.

Page 42, please amend the paragraph beginning at line 2 as follows:

In this Section we have described an interpolation method that we have devised

that uses trigonometric series for interpolation. Comparing the interpolations using the

trigonometric polynomial and the Lagrange polynomial of the same degree, the

trigonometric-based method achieves higher interpolation accuracy while simultaneously

reducing the computation time and the amount of required hardware. Moreover, the

trigonometric-based method ~~preforms~~ performs operations that are similar to ~~that~~ those

of a phase rotator for carrier phase ~~recovery~~ adjustment. This allows a reduction in the

overall synchronization circuit complexity by sharing resources.

Page 45, please amend the paragraph starting at line 19 as follows:

Since w is a rectangular function, W must be a sinc function 2210. Convolving F_c

and the sinc function W simply interpolates the frequency samples $\hat{F}(k)$ to obtain $F(\Omega)$,

$-\infty < \Omega < \infty$, shown as response 2212. (Here we have plotted the symmetric F only on

the positive half of the Ω axis.) We thus have

$$\hat{F}(k) = F(\Omega)|_{\Omega = 2\pi k/N}, \quad -\frac{N}{2} \leq k \leq \frac{N}{2}. \tag{3.8}$$

From response 2212, the continuous-frequency response $F(\Omega)$ is uniquely determined by

an infinite number of equally spaced frequency samples $\hat{F}(k)$. If we modify the

frequency samples 2214 near the passband edge to let the transition between the

passband and stopband be more gradual, as depicted in FIG. 23, then the ripple is

decreased. FIG. 23 demonstrates gradually reduced samples 2302, and the reduction of

ripples in the overall response 2304, as compared to the response 2212 in FIG. 22. The

cost of this improvement is[[,]] an increased transition bandwidth in the response 2304,

as compared to the response 2212.

Page 49, line 9, please replace Equation 3.21 with the following:

$$F(\Omega) = \left(\sum_{k=-M}^{M} \hat{F}(k)\delta\left(\Omega - \frac{2\pi}{N}\right) \right) \otimes \text{sinc}(\Omega)$$

$$= \sum_{k=-M}^{M} \hat{F}(k)\text{sinc}\left(\Omega - \frac{2\pi}{N}k\right). \tag{3.21}$$

Page 51, line 20, please replace equation 4.3 with the following:

$$F_d(\omega, \mu) = e^{j\omega\mu}$$

Page 59, please amend the paragraph beginning at line 21 as follows:

b.   Real $\hat{F}_\mu(1)$ values are used. The output of the angle-rotator ~~$\text{Re}\left(c_1 e^{j\frac{\pi}{2}\mu}\right)$~~

$\underline{\text{Re}\left(c_1 e^{j\frac{\pi}{2}\mu}\right)}$ is multiplied by $\hat{F}_\mu(1)$. Thus, one more real multiplexer is needed.

Page 68, please amend the two paragraphs starting at line 10 as follows:

The fine adjustment circuit 3804 generates a fine adjust value $(1 - \frac{1}{2}\underline{\theta_L}^2)$, where

θ_L is the least significant word of the input angle θ.

The second butterfly circuit 3810 multiples the output of circuit 3806 by θ_L^+ and

the fine adjustment value from circuit 3804, to perform a fine rotation that results in the

rotated complex number 3814. The + on the θ_L^+ denotes ~~the~~ that an error value $\Delta_{sin\theta_L}$ has

been added to improve the accuracy of the fine rotation.

Page 79, please amend the two paragraphs starting at line 12 as follows:

In step 4110, a fine adjustment circuit 3904 generates a fine adjust value

~~$\left(\delta_{[cos\theta_1]} - \theta_i^2\right)$~~ $\left(\delta_{[cos\theta_1]} - \frac{1}{2}\theta_i^2\right)$ based on the θ_i angle and $\delta_{[cos\theta_1]}$.

In step 4112, the butterfly circuit 3910 multiplies the intermediate complex signal

by the θ_i angle, and the fine adjustment value ~~$\left(\delta_{[cos\theta_1]} - \theta_i^2\right)$~~ $\left(\delta_{[cos\theta_1]} - \frac{1}{2}\theta_i^2\right)$ to perform a

fine rotation of the intermediate complex number, resulting in the output complex signal

3912.

Page 83, please amend the paragraph beginning at line 24 as follows:

For our structure, we chose the internal wordlengths and multiplier sizes as

indicated in FIG. 42. The phase-accumulator that generates [~~θ~~] $\overline{\theta}$ as well as the circuit

that maps an angle in the range [0, 2π] into [0, π/4], are described in (Madisetti, A.,

"VLSI architectures and IC implementation for bandwidth efficient communications,"

Ph.D. dissertation, University of California, Los Angeles (1996)). These structures are

also employed here in our test. Truncating the 32-bit phase word to 14 bits, this structure

has achieved a SFDR of 90.36 dB, as shown in FIG. 43. This is 6 dB better than the

single stage method.

Page 85, please amend equation 5.68 at line 5 to change the "-" sign in the second

equation to a "+" sign, an obvious error, as follows:

$$X_1 = X_0 - Y_0 \tan\theta_M$$
$$Y_1 = Y_0 + X_0 \tan\theta_M \qquad\qquad (5.68)$$

Page 89, please amend the two paragraphs beginning at line 23 as follows:

In step 4510, a fine adjustment circuit 4404 generates a fine adjust value

~~$\left(\delta_{[\cos\theta_1]} - \theta_l^2\right)$~~ $\left(\delta_{[\cos\theta_1]} - \frac{1}{2}\theta_l^2\right)$ based on the θ_l angle and $\delta_{\cos\theta_m}$.

In step 4512, the butterfly circuit 4410 multiplies the intermediate complex signal

by the θ_l angle, and the fine adjustment value ~~$\left(\delta_{[\cos\theta_1]} - \theta_l^2\right)$~~ $\left(\delta_{[\cos\theta_1]} - \frac{1}{2}\theta_l^2\right)$ to perform a

fine rotation of the intermediate complex signal, resulting in the output complex signal.

Page 98, please amend the section heading at line 5 as follows:

5.8.2.3 How to make a Conditionally ~~Negative~~ _Negating_ Booth

Multiplier

Page 128, please amend the paragraph beginning at line 11 as follows:

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The tangent, shown as the dashed line 7102, intersects the $f_1(Z) = X_1$ line at a new point Z_2. From Figure 70B, Z_2 is much closer to the desired value $1/X_1$ than the initial guess Z_1. Let us now find Z_2. According to Figure [[7-3]] 70B, we must have

Page 133, please amend the paragraph beginning at line 17 as follows:

In an embodiment where the invention is ~~implement~~ <u>implemented</u> using software, the software may be stored in a computer program product and loaded into computer system 7702 using removable storage drive 7714, hard drive 7712 or communications interface 7722. The control logic (software), when executed by the processor 7704, causes the processor 7704 to perform the functions of the invention as described herein.

Page 136, please replace equation B.2 at line 12 with the following:

$$c_k = \sum_{m=-N/2+1}^{N/2} \tilde{y}(m) W_{[m]\underline{N}}^{km} = \sum_{m=-N/2+1}^{N/2} \left(y(m) + mK \right) W_N^{km} \tag{B.2}$$

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Page 136, please replace equation B.3 with the following:

$$c_k = \sum_{m=-N/2+1}^{N/2} y(m)W_N^{km} - \sum_{m=-N/2+1}^{N/2} \left(m\frac{2}{N} \sum_{n=-N/2+1}^{N/2} (-1)^n y(n) \right) W_N^{km} \qquad \text{(B.3) (B.3)}$$

$$= \sum_{m=-N/2+1}^{N/2} y(m)W_N^{km} - \sum_{n=-N/2+1}^{N/2} \left(\sum_{m=-N/2+1}^{N/2} m\frac{2}{N}W_N^{km} \right)(-1)^n y(n)$$

$$= \sum_{m=-N/2+1}^{N/2} y(m)W_N^{km} - \sum_{m=-N/2+1}^{N/2} \left(\sum_{n=-N/2+1}^{N/2} n\frac{2}{N}W_N^{kn} \right)(-1)^m y(m)$$

Pages 138-139, please amend the paragraph beginning at page 138 line 18 as follows:

When we first discussed the interpolation problem in Section 2, we focused on interpolating between the two samples in the middle of the set of samples used to generate a synchronized sample. What is the impact on interpolation performance when we interpolate in an interval not at the center of the samples being used? Figure 74_shows such an example for $N = 4$, where the interpolation is performed between $y(0)$ and $y(1)$ using $y(-2)$, $y(-1)$, $y(0)$ and $y(1)$ (as opposed to using $y(-1)$, $y(0)$, $y(1)$ and $y(2)$, as seen in Figure 2 [[-1]] .